

Cambridge IGCSE[™]

	CANDIDATE NAME				
	CENTRE NUMBER		CANDIDATE NUMBER		
* 8 7	MATHEMATIC		0580/43		
0 1	Paper 4 (Extend	ded)	October/November 2022		
0 1			2 hours 30 minutes		
0 1 5	You must answe	er on the question paper.			
	You will need:	Geometrical instruments			

You will need: Geometrical instruments

INSTRUCTIONS

- Answer all questions. •
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs. •
- Write your name, centre number and candidate number in the boxes at the top of the page. •
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid. •
- Do not write on any bar codes. •
- You should use a calculator where appropriate. •
- You may use tracing paper.
- You must show all necessary working clearly.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in • degrees, unless a different level of accuracy is specified in the question.

This document has 20 pages. Any blank pages are indicated.

For π , use either your calculator value or 3.142.

INFORMATION

- The total mark for this paper is 130.
- The number of marks for each question or part question is shown in brackets [].

1 (a) Here are the ingredients needed to make a pasta bake to serve 12 people.

250g butter
600g pasta
460 g mushrooms
280g cheese
800 ml milk

(i) Find the mass of the cheese as a percentage of the mass of the mushrooms.

.....% [1]

(ii) Find the mass of butter needed to make a pasta bake to serve 18 people.

...... g [2]

(iii) Monica has 2.2 litres of milk and 1.5 kg of each other ingredient.

Calculate the greatest number of people she can serve with pasta bake.

......[3]

- (b) In 2019, a packet of pasta cost \$2.40. This was an increase of 25% of the cost of a packet in 2018.
 - (i) Work out the cost in 2018.

\$.....[2]

(ii) In 2020, the cost of a packet increased by 15% from the cost in 2019.

Work out the total percentage increase in the cost of a packet from 2018 to 2020.

.....% [3]

(c)

width	l ·		
			NOT TO
			SCALE

Pasta is sold in packets with width 11.5 cm, correct to the nearest 0.5 cm. A shop places these packets in a single line on a shelf of length 2 m, correct to the nearest 0.1 m.

Find the maximum number of these packets that will fit along this shelf. You must show all your working.

.....[3] [Turn over

2 (a)	Simplify	fully.
-------	----------	--------

(i)
$$p^3 \times p^{11}$$

(ii)
$$\frac{18m^6}{3m^2}$$

(iii)
$$\left(\frac{27x^9y^{27}}{64}\right)^{-\frac{1}{3}}$$

.....[3]

(b) A sequence has *n*th term $3n^2$.

Write down the first 3 terms of this sequence.

(c) Find the *n*th term for each of these sequences.

(i) 13, 16, 19, 22, 25, ...

......[2]

(ii) 3, 17, 55, 129, 251, ...

5

(d) Solve.

$$\frac{3x-22}{4} = 23$$

(e) Use the quadratic formula to solve $3x^2 + 8x - 20 = 0$. Show all your working and give your answers correct to 2 decimal places.

 $x = \dots, x = \dots$ [4]

3 The height, h cm, of each of 100 plants is recorded. The table shows information about the heights of these plants.

Height (<i>h</i> cm)	$10 < h \le 15$	$15 < h \leq 25$	$25 < h \leqslant 40$	$40 < h \le 60$	$60 < h \leqslant 70$
Frequency	8	18	28	33	13

(a) Complete the histogram to show this information. The first two blocks have been drawn for you.



(b) Calculate an estimate of the mean height.







NOT TO SCALE

The diagram shows a water trough in the shape of a prism. The prism has a cross-section in the shape of an isosceles trapezium. The trough is completely filled with water.

(a) Show that the volume of water in the trough is 206.4 litres.

[3]

(b) The water from the trough is emptied at a rate of 600 ml per second.

Calculate the time taken, in minutes and seconds, for the trough to be emptied.

..... minutes seconds [3]

(c) All the water from the trough is emptied into a vertical cylindrical tank. The depth of the water in the tank is 84 cm.



..... cm [3]

(i) Calculate the radius of the tank.

5

(ii) The tank is 60% full.

Calculate the height of the tank.



A steel rod AM is placed inside the empty water trough as shown in the diagram. A is a vertex at the base of the isosceles trapezium and M is the midpoint of the top edge on the opposite face.

Calculate the length of the steel rod, AM.

AM = cm [4]

[Turn over

6 (a) $P = 5k^2 - 7$

(i) Find the value of *P* when k = 3.

(ii) Rearrange the formula to make *k* the subject.

 $k = \dots$ [3]

(b) (i) Solve. $x-3 \le 5x+7$

......[2]

(ii) Show your answer to **part** (b)(i) on the number line.



(c) The line y = 16 is drawn on the grid.



The region R satisfies the following inequalities.

 $y \ge 16 \qquad x > 2 \qquad 2x + 3y \ge 72 \qquad y \le 32 - x$

(i) By drawing three more lines and shading the region **not required**, find and label region *R*. [6]

(ii) Find the integer coordinates (x, y) in the region R that give the maximum value of 2x + y.

(.....) [2]

7 Regan is playing a game with these six number cards.



(a) She takes two cards at random, without replacement, and **multiplies** the two numbers to give a score.

Find the probability that

(i) the score is 35

......[3]

(ii) the score is a positive number.

(b) Regan now takes three cards at random from the six cards, without replacement, and **adds** the three numbers to give a total.

Find the probability that her total is 5.

......[4]



A, B and C are points on the circle, centre O. DE is a tangent to the circle at C. AC = 10 cm, AB = 9.5 cm and BC = 7.7 cm.

(a) Show that angle $ABC = 70.2^{\circ}$, correct to 1 decimal place.

- (**b**) Find
 - (i) angle *AOC*
 - (ii) angle ACO

Angle $ACO = \dots$ [1]

Angle $AOC = \dots$ [1]

(iii) angle ACD.

- Angle *ACD* = [1]
- (c) Calculate the radius, *OC*, of the circle.

OC = cm [3]

(d) Calculate the area of triangle *ABC* as a percentage of the area of the circle.

.....% [4]

9 (a) Sketch the following graphs. On each sketch, indicate any intercepts with the axes.



[2]

(b) (i) Find the derivative,
$$\frac{dy}{dx}$$
, of $y = 5 + 8x - \frac{4}{3}x^3$.

(ii) Find the gradient of $y = 5 + 8x - \frac{4}{3}x^3$ at x = -1.

(iii) A tangent is drawn to the graph of $y = 5 + 8x - \frac{4}{3}x^3$. The gradient of the tangent is -28.

Find the coordinates of the two possible points where this tangent meets the graph.

(.....) (.....) [5]

10 (a)
$$\mathbf{a} = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$$
 $\mathbf{b} = \begin{pmatrix} -3 \\ 5 \end{pmatrix}$

(i) On the grid, draw and label vector 2a.



(ii) On the grid, draw and label vector $(\mathbf{a} - \mathbf{b})$.

			r				
1	1						
1	1	1	1	1	1	1	
1	1					1	
i.	i	i			i i		
1							
1	1						
1	1						
1	1					1	
1	1				1	1	
1	1						
1	1						
1	1	1					
1	1					1	
1	1						
1	1						
1	1						
1	1	1					
1	1	1				1	
1	1				1		
1							
	+						
	1						
1	1	1	1		1	1	
1	1	1					
1	1						
1							
1	1				1		
1	1		1		1		
1	1	1	1	1	1	1	
1	1				1		
i	i				i		
L							
1	1	1	1		1	1	
1	1					1	
1	1				1	1	
1	1						
1	1						
1	1	1					
1	1	1				1	
1	1				1	1	
1							
1	1						
L	4						
1	1	1	1				
1	1					1	
1	1				1		
1							
1	1						
1	1	1	1				
1	1					1	
1	1				1	1	
i.	i	i					
1	1						
1	1						
1	1	1	1		1	1	
1	1					1	
1	1				1		
i	i						
:	:		:			:	
1	1		5		5		
1	1						
1	1	1	1		1		1
1	1	1			1	1	
L	4						Lanana I
1							
1	:						
1	1						
1	1	1	1		1		
1	1	1			1	1	
1	1				1		
i	i						
1	:						
1	1						
1	1	1	1		1	1	
r	+		+			1	
1	1				1		
i	i						
1	:						
1	1						
1	1	1	1		1	1	
1	1	1			1	1	
1							
1	:		:				
1	1						
1	1	1	1		1	1	
L	4						

[2]

[1]



OABC is a trapezium with *OA* parallel to *CB*. *M* is the midpoint of *CB* and *N* is the point on *AB* such that AN : NB = 1 : 2. *O* is the origin, $\overrightarrow{OA} = \mathbf{p}$, $\overrightarrow{OC} = \mathbf{q}$ and $\overrightarrow{CB} = \frac{3}{4}\mathbf{p}$.

- (i) Find, in terms of **p** and/or **q**, in its simplest form
 - (a) \overrightarrow{OB}

(**b**) \overrightarrow{AB}

 $\overrightarrow{AB} = \dots \qquad [2]$

(c) \overrightarrow{MN} .

(ii) OA and MN are extended to meet at G.

Find the position vector of *G* in terms of **p**.

BLANK PAGE

Permission to reproduce items where third-party owned material protected by copyright is included has been sought and cleared where possible. Every reasonable effort has been made by the publisher (UCLES) to trace copyright holders, but if any items requiring clearance have unwittingly been included, the publisher will be pleased to make amends at the earliest possible opportunity.

To avoid the issue of disclosure of answer-related information to candidates, all copyright acknowledgements are reproduced online in the Cambridge Assessment International Education Copyright Acknowledgements Booklet. This is produced for each series of examinations and is freely available to download at www.cambridgeinternational.org after the live examination series.

Cambridge Assessment International Education is part of Cambridge Assessment. Cambridge Assessment is the brand name of the University of Cambridge Local Examinations Syndicate (UCLES), which is a department of the University of Cambridge.